

TRANSACTION & CONCURRENCY CONTROL

Read(Q): Accessing data item (Q)

Write(Q): Updating the data item (Q).

Commit: Commit indicates Completion of transaction Successfully.

→ A transaction is a unit of program execution that accesses and possibly update various data items.

eg: Transfer Rs 500 from Account A to Account B.

1. read(A) 4. read(B)

2. $A = A - 1000$ 5. $B = B + 1000$

3. write(A) 6. write(B)

→ To Preserve the integrity of data the database system must ensure:

1. Atomicity

2. Consistency

3. Isolation

4. Durability

ACID

Property

Atomicity: Either all operations of the transaction are properly reflected in the database or none.

{ Full or None }.

Reasons of Failure:

* System Failure

* Software Crash

* Hardware Crash... etc.

* Due to any of these reason if transaction is failed before commit then Recovery management Component are there.

* When a transaction is failed Recovery management Component Rollbacks (undo all modifications).

* Log (Transaction log): it contains all the activity (modifications) of the transaction.

Consistency: Execution of transaction T in isolation preserves the Consistency of the database. In other words, before and after the transaction, the database must be consistent.

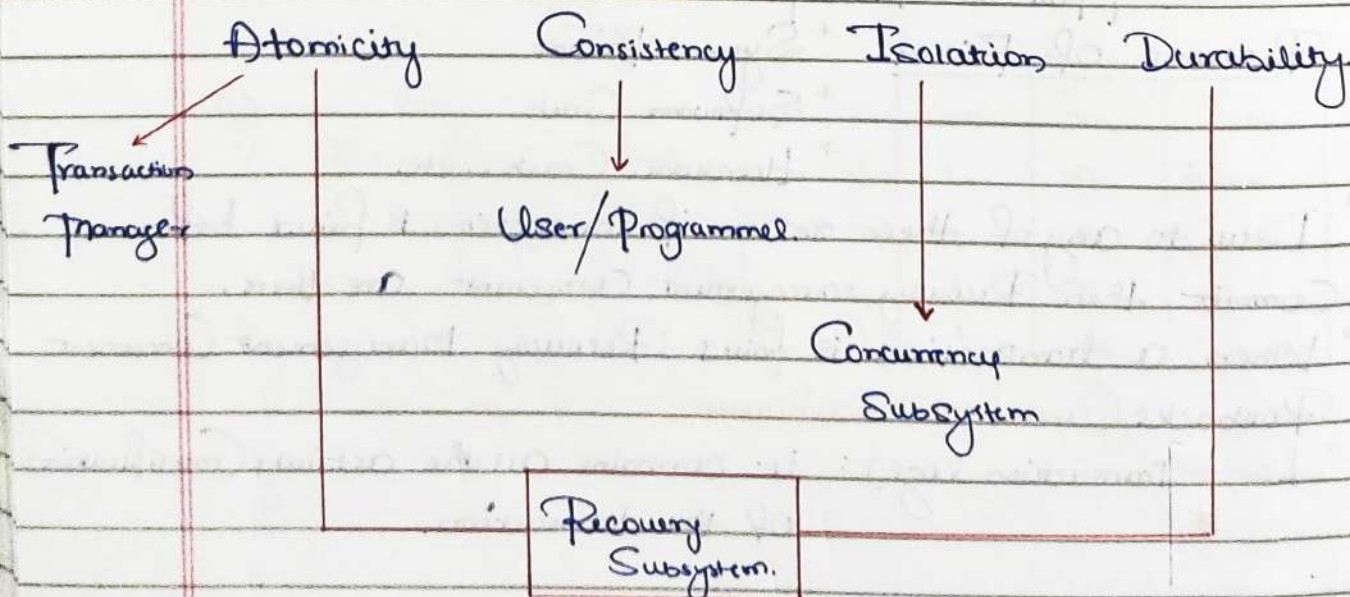
Isolation: Although multiple transactions may execute concurrently, each transaction must be unaware of other concurrently executing transactions. Intermediate transaction results must be hidden from other concurrently executed transactions.

* When two or more transactions execute concurrently then isolation comes into picture.

* Concurrent execution of two or more transactions should be equal to any serial schedule.

Durability: Any change in the database must persist for a long period of time.

Database must be able to recover under any case of failure.



Transaction State:

Active: the initial state, the transaction stays in this state while it is executing.

Partially Committed: after the final statement has been executed.

Failed: after the discovery that no longer the normal execution can proceed.

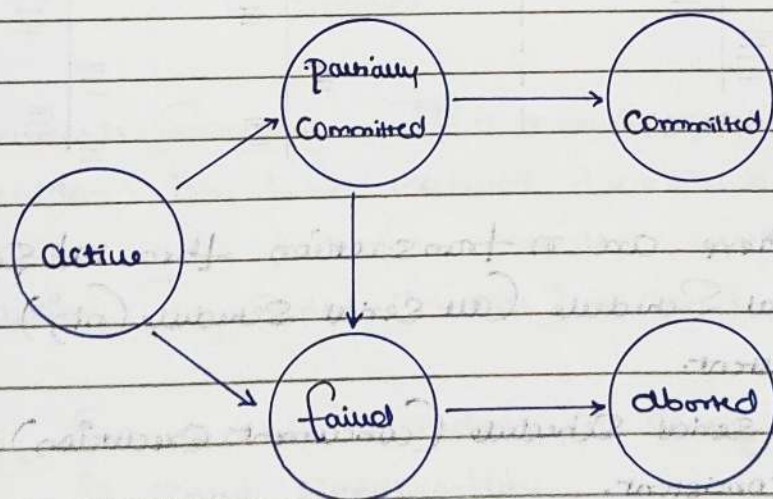
Aborted: After the transaction has been rolled back and the database restored to its state prior to the start of the transaction.

Two options after it is aborted:

(i) Restart the transaction - can be done if no internal logical error.

(ii) Kill the transaction.

Committed: After successful completion.



Schedule: a sequence of instructions that specify the chronological order in which instructions of current transactions are executed.

* A schedule for a set of transactions must consist of all instructions of those transactions.

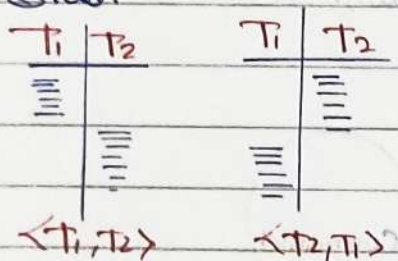
* Must preserve the order in which the instructions appear in each individual transaction.

- A transaction that successfully completes its execution will have a commit instruction as the last statement.
- * By default the transactions assumed to execute commit instruction as its last step.
- A transaction that fails to successfully complete its execution will have an abort instruction as its last statement.

Schedule { Time order sequence of two or more transaction }.

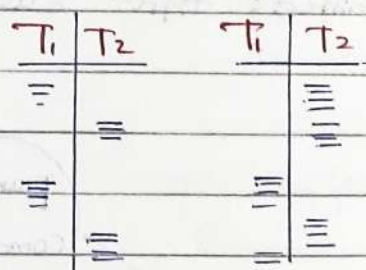
① Serial Schedule -

Execution of one transaction successfully, then other will start.



② Non Serial Schedule { Concurrent Execution }

Interleaved execution of two or more transaction.



Note: * If there are n transaction then $n!$ Serial Schedule.

* Serial Schedule (all Serial Schedule ($n!$)) are always consistent.

* Non-Serial Schedule (concurrent execution) may or may not be consistent.

* But we execute concurrent execution.

Q₁. Why Concurrent Execution?

- * To improve CPU utilization
- * Enhanced throughput
- * Fast response, less waiting time.
- * Effective utilization of Resource.

Serial Schedule:

- * After commit of one transaction, begin (start) another transaction.
- * Number of possible serial schedules with 'n' transactions is "n!".
- * The execution sequence of serial schedule always generates consistent result.
- * Example: $R_1(A)$ $W_1(A)$ Commit (T_1) $R_2(A)$ $W_2(A)$ Commit (T_2)

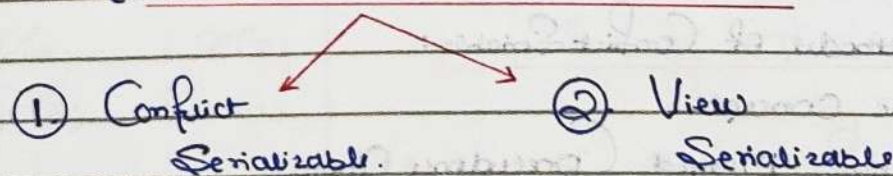
Advantage: Serial schedule always produce correct result (integrity guaranteed) as no resource sharing.

Disadvantages:

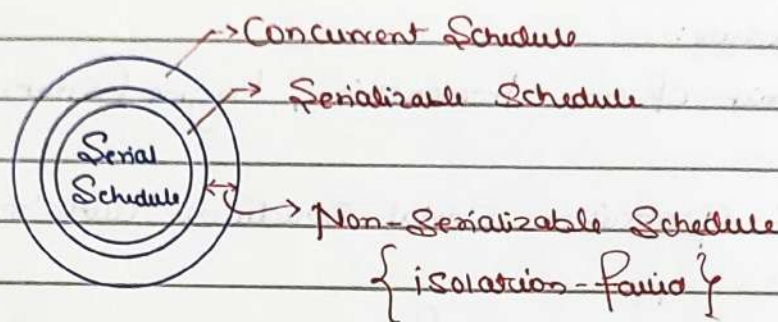
- * Less degree of concurrency.
- * Throughput of system is low.
- * It allows transaction to execute one after another.

Serializable Schedule: If a non serial schedule (concurrent execution) has been executed, that could have same effect on database as a schedule executed without any concurrent execution (any serial schedule), is called Serializable Schedule.

Note: Serializable Schedules are always consistent. This process is called Serializability.

How to achieve Serializable Schedule

- * A schedule is Serializable if it is equivalent to a serial schedule.



Serializability:

Basic assumption: Each transaction preserves database consistency.
 Thus, serial execution of a set of transactions preserves database consistency.

A (possibly concurrent) schedule is serializable if it is equivalent to a serial schedule. Different forms of schedule equivalence give rise to the notions of

- ① Conflict Serializability.
- ② View Serializability.

Conflict Serializable:

Let us consider schedule S_1 in which there are two consecutive instructions T_i and T_j of transactions T_i and T_j respectively [if]

Same data item

→ No Conflict operation/instruction.

T_i T_j

$R(A) \rightarrow W(A)$

$W(A) \rightarrow R(A)$

$W(A) \rightarrow W(A)$

[Swapping not possible]

T_i T_j

$R(A) \rightarrow R(A)$

$R(A) \rightarrow W(B)$

Different data item

[Swapping possible]

Methods of Conflict Serializability:

1. Basic Concept.
2. Testing Method (Precedence Graph)
3. Conflict Equal to any Serial Schedule

S : Non Serial Schedule
[Given Question]

S' : Any Serial Schedule of S
(of Given questions).

$S \xrightarrow{\text{by Series of Swap of non Conflicting instructions.}} S'$

$\rightarrow$ then the Schedule ' S ' is Conflict Serializable.

* If a Schedule S can be transformed into a Schedule S' by a Series of Swaps of non-conflicting instructions, we say that S and S' are Conflict equivalent.

* We say that a Schedule is Conflict Serializable if it is Conflict equivalent to any Serial Schedule.

Q1.

T_1	T_2	T_1	T_2
$R(A)$		$R(A)$	
$W(A)$		$W(A)$	
	$R(A)$	$R(B)$	
	$W(A)$	$W(B)$	
$R(B)$		$R(A)$	
$W(B)$		$W(A)$	
	$R(B)$	$R(B)$	
	$W(B)$	$W(B)$	

$S: \langle \text{Given} \rangle$ $S': \langle T_2, T_1 \rangle$

Annotations:
 - Swap Conf. be done $\rightarrow$ (between $W(A)$ and $R(A)$ in T_2)
 - not possible by swapping $\rightarrow$ (between $R(A)$ and $R(B)$ in T_2)
 - not possible. $\rightarrow$ (between $W(A)$ and $R(B)$ in T_2)

$\rightarrow$ Here ' S ' can't be converted into ' S' ' $\langle T_2, T_1 \rangle$ by swapping T_2 followed by T_1 .
 $\therefore S$ is not Conflict Serializable.

Q1.

T_1	T_2	T_1	T_2
$R(A)$		$R(A)$	
$W(A)$		$W(A)$	
	$R(A)$	$R(B)$	
	$W(A)$	$W(B)$	
$R(B)$		$R(A)$	
$W(B)$		$W(A)$	
	$R(B)$	$R(B)$	
	$W(B)$	$W(B)$	

$S: \langle \text{Given} \rangle$ $S': \langle T_1, T_2 \rangle$

Annotations:
 - Possible to convert $\rightarrow$ (between $W(A)$ and $R(A)$ in T_2)
 - Swap allowed $\rightarrow$ (between $W(A)$ and $R(A)$ in T_2)
 - different $\rightarrow$ (between $R(A)$ and $R(B)$ in T_2)
 - no conflict $\rightarrow$ (between $W(A)$ and $R(B)$ in T_2)

$\rightarrow$ Here S can be converted into ' S' ' $\langle T_1, T_2 \rangle$ by swapping T_1 followed by T_2 .
 $\therefore S$ is Conflict Serializable.

Conflicting Instructions:

- * Instructions I_i and I_j of transactions T_i and T_j respectively, Conflict if and only if there exists some item Q accessed by the both I_i and I_j and at least one of these instructions write (Q).

1. $I_i = \text{read}(Q), I_j = \text{read}(Q) \rightarrow$ non conflict instructions
2. $I_i = \text{read}(Q), I_j = \text{write}(Q)$
3. $I_i = \text{write}(Q), I_j = \text{read}(Q)$
4. $I_i = \text{write}(Q), I_j = \text{write}(Q)$

} they
conflict.

- * Intuitively, a conflict between I_i and I_j forces a (logical) temporal order between them.

- * If I_i and I_j are consecutive in a schedule and they do not conflict, their results could remain the same even if they had been interchanged in the schedule.

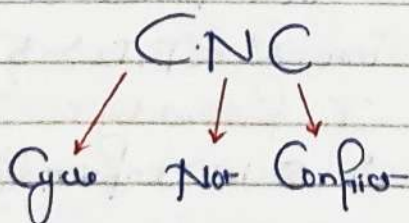
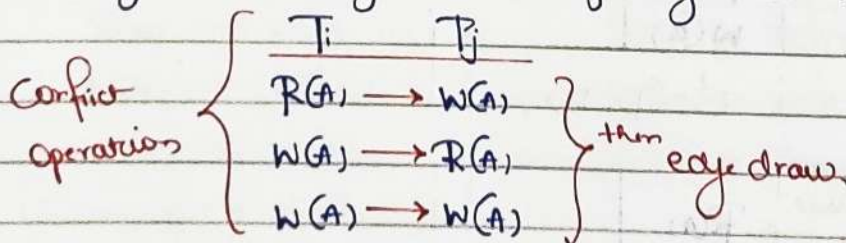
Testing for Serializability:

Precedence Graph Method:

$G(V, E)$

(Vertex) V : Set of transactions.

(Edge) E : Edge $T_i \rightarrow T_j$ edge occur if any one condition hold.



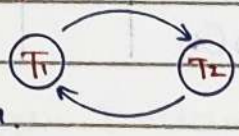
Note: If precedence graph contains cycle (any one cycle) then schedule is not Conflict Serializable!

Testing for Conflict Serializability

- * Consider some schedule of a set of transactions $T_1, T_2, \dots, T_n$
- * Precedence Graph: a directed graph where the vertices are the transactions (names).
- * We draw an arc from T_i to T_j if the two transactions conflict and T_i accessed the data item on which the conflict arises earlier.
- * We may label the arc by the item that was accessed.

eg:  A schedule is Conflict Serializable if and only if its precedence graph is acyclic.

Q1.	T_1	T_2		T_1	T_2
	$R(A)$			$R(A)$	
	$w(A)$				$R(A)$
		$R(A)$	Acyclic		$w(A)$
		$w(A)$	$\therefore$ Conflict Serializable		$w(A)$
	$R(B)$		$\langle T_1, T_2 \rangle$		$R(B)$
	$w(B)$				$w(B)$
		$R(B)$			$R(B)$
		$w(B)$			$w(B)$

Q2.	T_1	T_2		T_1	T_2
	$R(A)$				
	$w(A)$		$\therefore$ Not Conflict Serializable		
		$R(B)$			
		$w(B)$			
	$R(B)$				
	$w(B)$				
		$R(A)$			
		$w(A)$			

 Cycle
 $\therefore$ Not Conflict Serializable

Q3. Consider the following Schedule involving two transactions. Which of the following is true?

$S_1: r_1(x), r_1(y), r_2(x), r_2(y), w_2(y), w_1(x).$
 $S_2: r_1(x), r_2(x), r_2(y), w_2(y), r_1(y), w_1(y).$

Ans

T_1	T_2
$r(x)$	
$r(y)$	
	$r(x)$
	$r(y)$
	$w(y)$
$w(x)$	

Diagram for S_1 : $T_1 \rightarrow T_2 \rightarrow T_1$ (Cycle)
 $\therefore$ Not Conflict
 Serializable(S_1)

T_1	T_2
$r(x)$	
	$r(x)$
	$r(y)$
	$w(y)$
$r(y)$	
$w(x)$	

Diagram for S_2 : $T_2 \rightarrow T_1$ (Cycle)
 $\therefore S_2$ Conflict
 Serializable

$\Rightarrow S_1$ not conflict and S_2 is Conflict Serializable.

Q4. Consider the following four schedules due to three transactions (indicated by subscript) using read and write on data item x , denoted by $r(x)$ and $w(x)$ respectively. Which of them is conflict Serializable?

Ans

T_1	T_2	T_3
	$r(x)$	
	$w(x)$	
$r(x)$		$r(x)$
$w(x)$		

Diagram: $T_2 \rightarrow T_1$ (Not Cyclic), $T_2 \rightarrow T_3 \rightarrow T_1$ (A Cyclic)
 $\therefore$ Conflict Serializable
 $\langle T_2, T_3, T_1 \rangle$

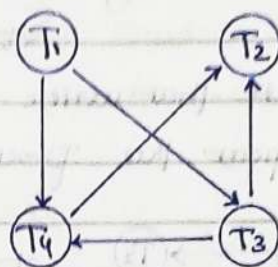
$\Rightarrow r_2(x), w_2(x), r_3(x), r_1(x), w_1(x).$

Q5. Let $R_i(z)$ and $W_i(z)$ denote read and write operations on data element z by transaction T_i , respectively. Consider the Schedule S with for transactions.

$S: R_1(x), R_2(x), R_2(x), R_1(y), W_1(y), W_2(x), W_3(y), R_4(y).$

Which of the following serial Schedules is conflict equivalent to S ?

T_1	T_2	T_3	T_4
	$R(x)$	$R(x)$	$R(y)$
$R(y)$ $w(y)$			
	$w(x)$	$w(y)$	$R(y)$



$\Rightarrow \langle T_1, T_3, T_4, T_2 \rangle$

Method-II

$S: R_4(x), R_2(x), R_3(x), R_1(y), w_1(y), w_2(x), w_3(y), R_4(y)$

Data item (x) : $R_4(x) - w_2(x) : T_4 \rightarrow T_2$
 $R_3(x) - w_2(x) : T_3 \rightarrow T_2$

Data item (y) : $R_1(y) - w_3(y) : T_1 \rightarrow T_3$
 $w_1(y) - w_3(y) : T_1 \rightarrow T_3$
 $w_1(y) - R_4(y) : T_1 \rightarrow T_4$
 $w_3(y) - R_4(y) : T_3 \rightarrow T_4$

$T_1 \rightarrow T_3 \rightarrow T_4 \rightarrow T_2$

Serializability Order

If schedule is Conflict Serializable (Acyclic Precedence graph) then Serializability order indicate (true) that non Serial Schedule is equivalent to which Serial Schedule.

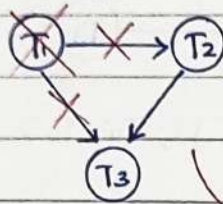
eg: 1. Serializability order
 $\langle T_1, T_2 \rangle$

2. $\langle T_2, T_1 \rangle$ is equivalent to Serial schedule T_2 followed by T_1

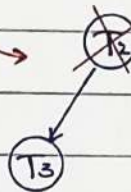
Topological Sorting: (Process)

Start from the vertex which having $\text{Indegree} = 0$ (no incoming edge) then delete that vertex and all connecting edge from that vertex and repeat this process until complete graph (all vertex) traversed.

eg:



Indegree = 0 (no incoming edge)

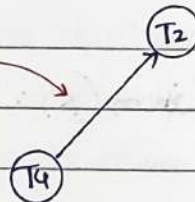
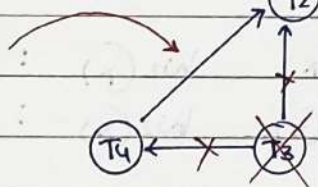
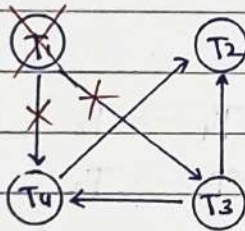
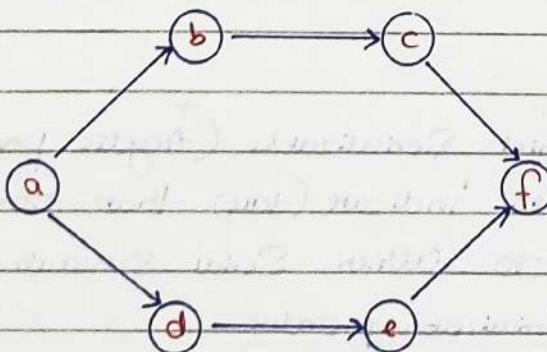
 T_1 

Indegree = 0

 $\Rightarrow \langle T_1, T_2, T_3 \rangle$

Serializability Order.

eg:

Serializability Order: $\langle T_1, T_3, T_4, T_2 \rangle$ Homework: How many topological Sorting order possible.

Conflict Equivalence:

Two Schedules are said to be Conflict equivalent, if all conflicting operations in both the schedules could be executed in the same order.

eg: $S_1: R_1(x), W_1(x), R_2(y), W_2(y), R_1(y)$
 $S_2: R_1(x), W_1(x), R_1(y), R_2(y), W_2(y)$

T_1	T_2		T_1	T_2	
$R(x)$		<u>Conflict operation:</u> $W(y) - R(y) : T_2 \rightarrow T_1$ <u>or</u> $W_2(y) \rightarrow R_1(y)$ $: T_2 \rightarrow T_1$	$R(x)$		$R(y) - W(y)$
$W(x)$			$W(x)$		$: T_1 \rightarrow T_2$
	$R(y)$		$R(y)$		<u>or</u>
	$W(y)$			$R(y)$	$R_1(y) - W_2(y)$
$R(y)$				$W(y)$	$T_1 \rightarrow T_2$

$\rightarrow S_1$ is not Conflict equivalent to S_2

eg: 2 $S_1: R_1(A) W_1(A) R_2(A) W_2(A) R_1(B) W_1(B)$
 $S_2: R_1(A) W_1(A) R_2(A) R_1(B) W_2(A) W_1(B)$

T_1	T_2	
$R(A)$		$R(A) - W(A) : T_1 \rightarrow T_2$
$W(A)$		$W(A) - R(A) : T_1 \rightarrow T_2$
		$W(A) - W(A) : T_1 \rightarrow T_2$
	$R(A)$	<u>or</u>
	$W(A)$	$R_1(A) - W_2(A) : T_1 \rightarrow T_2$
$R(B)$		$W_1(A) - R_2(A) : T_1 \rightarrow T_2$
$W(B)$		$W_1(A) - W_2(A) : T_1 \rightarrow T_2$

$R(A)$		$R(A) - W(A) : T_1 \rightarrow T_2$
$W(A)$		$W(A) - R(A) : T_1 \rightarrow T_2$
	$R(A)$	$W(A) - W(A) : T_1 \rightarrow T_2$
		<u>or</u>
$R(B)$		$R_1(A) - W_2(A) : T_1 \rightarrow T_2$
	$W(A)$	$W_1(A) - R_2(A) : T_1 \rightarrow T_2$
$W(B)$		$W_1(A) - W_2(A) : T_1 \rightarrow T_2$

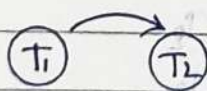
S_1 is Conflict equivalent to S_2

Conflict Serializable: A schedule is said to be Conflict Serializable if it is conflict equivalent to a Serial schedule.

Same Conflicting Operation Order in G_1 & S_1 . ∴ Its $\{G_1\}$ Conflict is Conflict Serializable.	T_1	T_2	T_1	T_2
	read(A)		read(A)	
	write(A)		write(A)	
		read(A)	read(B)	
		write(A)	write(B)	
	read(B)			read(A)
	write(B)			write(A)
		read(B)		read(B)
		write(B)		write(B)

Important Note:

- ① If S_1, S_2 schedule are conflict equal then precedence graph of S_1 and S_2 must be same.
- ② If S_1 and S_2 have same precedence graph then S_1 and S_2 may or may not be conflict equal.

eg:	<u>S₁</u>		<u>S₂</u>	
	<u>T₁</u>	<u>T₂</u>	<u>T₁</u>	<u>T₂</u>
	W(A)		W(C)	
		R(A)		R(C)
				
		Precedence Graph is		
		Same but not		
		conflict equal		
		{S ₁ , S ₂ }		

Serializable:

- ① A schedule is Serializable if either it is Conflict Serializable or
- ② View Serializable or both.

Note: * If schedule is Conflict Serializable (Acyclic graph) then already it is view Serializable.
* If schedule is not Conflict Serializable (CNC) then it may or

may not be Serializable.

* If Schedule is view Serializable but not conflict then schedule is Serializable. (Consistent)

* If Schedule is not conflict and not view then schedule is not Serializable Schedule. (Inconsistent)

* If conflict ✓
then already
view satisfy ✓

* If not conflict Serializable (CNC)

View Satisfy

↓
Serializable

View Fail (not satisfy)

↓
Not Serializable

Serializable

① Conflict Serializable

② View Serializable

On each data
item

1. Initial read

2. Final write

3. Updared read (write read
Sequence).

Equivalent Schedule

1. Result Equivalent: Two schedule are said to be result equivalent if they produce same final result for some initial value of data.
eg: $A = 100$

S₁
Read(A)
 $A = A + 10$
 $110 \leftarrow$ Write(A)

S₂
Read(A)
 $A = A * 1.1$
Write(A) $\Rightarrow 110$

* S₁ and S₂ are Result
Equivalent.

2. Conflict Equivalent

3. Complete Schedule: A Schedule is said to be complete schedule if last operation of each transaction is either commit or abort.
Could complete schedule otherwise Partial schedule.

View Serializability.

Let S and S' be two Schedules with the same set of transactions. S and S' are view equivalent if following three conditions are met: for each data item Q :

1. If in Schedule S , transaction T_i reads the initial value of Q , then in Schedule S' also transaction T_i must read the initial value of Q .
2. If in Schedule S transaction T_i executes read(Q), and the value was produced by transaction T_j (if any), then in Schedule S' also transaction T_i must read the value of Q that was produced by the same write(Q) operation of Transaction T_j .
3. The transactions (if any) that perform the final write(Q) operations in Schedule S must also perform the final write(Q) operations in Schedule S' .

View Equivalent: S_1 and S_2 are said to be equivalent only if

- (i) Initial reads of S_1 and S_2 should be same.
- (ii) Final updations for every data item should be same in S_1 and S_2 .

S_1			S_2		
T_1	T_2	T_3	T_1	T_2	T_3
R(A)				W(A)	
R(B)			R(A)		
	W(B)		R(B)		
		W(A)			W(B)

$S_1 \neq S_2$

- (iii) Write-Read Sequence should also be equal. (Updated reads should be same).

eg:

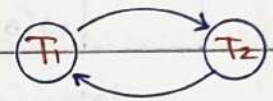
T ₁	T ₂
R(A)	
W(A)	
	R(A)
	W(A)
R(B)	
W(B)	
	R(B)
	W(B)

Schedules: $\langle T_1, T_2 \rangle$ ✓× $\langle T_2, T_1 \rangle$

Conflict Serializable $\langle T_1, T_2 \rangle$
and it is already "view serializable".

eg: 2

T ₁	T ₂	T ₃
	R(A)	
	R(B)	
W(B)		
		R(B)
W(A)		
	W(A)	
		W(A)



T₃ Cycle
- No Conflict

But it is view equivalent.

T ₁	T ₂
R(A)	
W(A)	
	R(A)
	W(A)
R(B)	
W(B)	
	R(B)
	W(B)

① Initial Read

A: T₁B: T₁

② Final Write

A: T₂B: T₂

③ Write-Read (updated Read)

T ₁	T ₂
R(A)	
W(A)	
R(B)	
W(B)	
	R(A)
	W(A)
	R(B)
	W(B)

① Initial Read

A: T₁B: T₁

② Final Write

A: T₂B: T₂③ Updated Read
(write-read Sequence)A: w₁(A) - R₂(A) : T₁ → T₂B: w₁(B) - R₂(B) : T₁ → T₂A: w₁(A) - R₂(A) : T₁ → T₂B: w₁(B) - R₂(B) : T₁ → T₂it's view serializable $\langle T_1, T_2 \rangle$

eg: 3

T ₁	T ₂
R(A)	
	R(A)
	W(A)
W(A)	
R(B)	
W(B)	
	R(B)
	W(B)

Dummy. $\langle T_1, T_2 \rangle$ (fair as final write).
 $\times \langle T_2, T_1 \rangle$ (fair as initial read)

- ① Initial Read
A: T₁, T₂
B: T₂
- ② Final Write
A: T₁
B: T₂

R(A)	
W(A)	
R(B)	
W(B)	
	R(A)
	W(A)
	R(B)
	W(B)

- ① Initial Read
B: T₁
A: Only T₁ not T₂
- ② Final Write
A: T₂ } fair.

- Not Conflict
- Not View Serializable.

eg: 4

T ₁	T ₂	T ₃
R(A)		
	W(A)	
W(A)		
		W(A)

T ₁	T ₂	T ₃
R(A)		
W(A)		
	W(A)	
		W(A)

1. Initial Read A: T₁
 2. Final Write A: T₃
- No write-Read
(no updated Read)

1. Initial Read : A: T₁
 2. Final Write A: T₃
- (no updated Read)

∴ Not Conflict but view Serializable
 ∴ Serializable.

eg: 5

T ₁	T ₂	T ₃
	R(A)	
	R(B)	
W(B)		
		R(B)
W(A)		
	W(A)	
		W(A)

- Dummy
 $\langle T_2, T_1, T_3 \rangle$
- ① Initial Read
A: T₂, B: T₂
 - ② Final write on
A: T₃ B: T₁
 - ③ Updated Read
T₁ → T₃

T ₁	T ₂	T ₃
	R(A)	
	R(B)	
	W(A)	
W(B)		
W(A)		
		R(B)
		W(A)

- ① Initial Read
A: T₂, B: T₂
- ② Final write on
A: T₃, B: T₁
- ③ Updated Read
T₁ → T₃

Not Conflict but view Serializable.

Problem due to Concurrent Execution:

1. WR (Write-Read) / Uncommitted Read / Dirty Read Problem.
2. RW (Read-write) / Non/un repeatable read problem.
3. WW (write-write) / lost update formula.
4. Phantom Tuple Problem

Finding total number of schedule.

Concurrent Schedule { Serial Schedule + Non Serial Schedule }

→ m Transactions.

Total number of Serial Schedule = $m!$ Serial Schedule

$$\text{Non Serial Schedule} = \text{Total Concurrent Schedule} - \text{Serial Schedule (m!)} \quad \begin{matrix} \text{m: no. of} \\ \text{transaction} \end{matrix}$$

eg: T_1 T_2 $\left\{ \begin{array}{l} L_1 L_2 L_3 L_4 \\ L_3 L_4 L_1 L_2 \\ L_1 L_3 L_2 L_4 \text{ or } L_1 L_2 L_4 L_2 \\ L_3 L_4 L_1 L_2 \text{ or } L_3 L_4 L_2 L_4 \end{array} \right.$

$T_1 - n_1$ Operation

$T_2 - n_2$ Operation

$$\text{Total no. of Concurrent Schedule} = \frac{(n_1 + n_2)!}{(n_1)! (n_2)!}$$

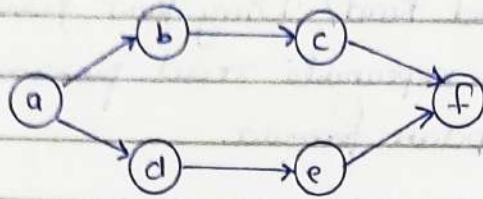
$$\text{Concurrent Schedule} = \frac{(n_1 + n_2)!}{(n_1)! (n_2)!}$$

The number of Concurrent schedule that can be formed over m transactions having $n_1, n_2, n_3, \dots, n_m$ Operations respectively.

$$\text{Total no. of concurrent Schedule} = \frac{(n_1 + n_2 + n_3 + \dots + n_m)!}{(n_1)! (n_2)! (n_3)! \dots (n_m)!}$$

$$\text{Total no. of non Serial Schedule} = \frac{(n_1 + n_2 + n_3 + \dots + n_m)!}{(n_1)! (n_2)! (n_3)! \dots (n_m)!} - m!$$

Q1. Consider the following directed graph:



The no. of different topological ordering of the vertices of graph is 6.

| a b c d e f
 | a d e b c f
 | a b d c e f
 | a b d e c f
 | a d b e c f
 | a d b c e f

Q2. Consider the following transaction involving two bank accounts x & y .
 $read(x)$, $x = x - 50$, $write(x)$, $read(y)$, $y = y + 50$, $write(y)$.
 The constraint that the sum of accounts x and y should be constant is that of.

Ans Consistency.

Q3. Which of the following is not a part of the ACID properties of database transactions?

Ans Deadlock-freedom.

① Write-Read Problem / Uncommitted / Dirty Read Problem.

T_1	T_2
$w(A)$	$r(A)$

UnCommitted / Dirty Read: Here T_2 read the value of data item (A) that is updated (written) by uncommitted transaction T_1 .

② R/w Problem / Non / Un Repeatable Read.

T_1	T_2
$r(A)$	$w(A)$

eg:

T_1	T_2
$A = 10$ $Read(A)$ $if(A \neq 0)$ $\{$ $10 - 1 = 9.$ $A = 9 - 1$ $write(A)$ $\}$	$A = 10$ $Read(A)$ $if(A \neq 0) \{ A = A - 1, A = 9.$ $write(A) \}$

9 book in store
 + 2 books issued
 11. $\rightarrow$ Inconsistency

③ WW Problem / Lost update Problem:

T ₁	T ₂	T ₁	T ₂
W(A)		Read(A)	
	$A = 1000$	$A = A + 100$	
			Read(A) $\rightarrow A = 1000$
			$temp = A * 0.1$ $temp = 100$
			$A = A + temp$
	$A = 900$		
	Write(A)		
			Write(A) $A = 1100$

Suppose the operation of transaction T₁ and T₂ is such a manner T₂ read the value of Account(A) before T₁ update and T₂ update, the value of account just after T₁ update.

So whenever update done by T₁ is overwritten by the later transaction (So lose of updation of T₁ transaction).

Last update Checking: If there are two write operation of different transactions and between these two write there is no read operation, then Second (later) transaction overwrites the value of first transaction is called lost update.

④ Phantom Tuple Problem

eno.	ename.	esal
e1	A	5000
e2	B	6000
e3	D	7000

Select*
From Employee
Where Salary > 4700

eno.	ename.	esal
e1	A	5000
e2	B	6000
e3	D	7000
e5	E	6700

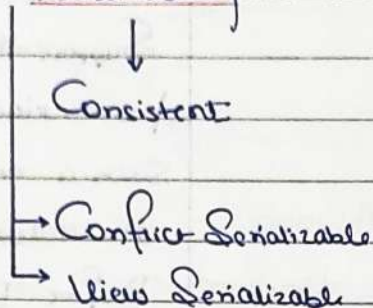
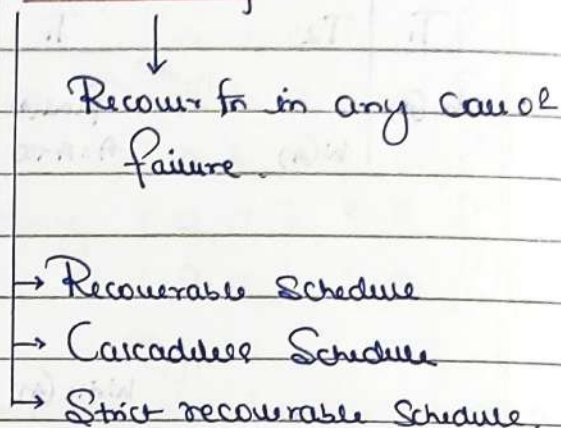
Select*
From Employee
Where
Salary > 4700

→ Phantom tuple

Employee

eno.	ename	esalary
e1	A	5000
e2	B	6000
e3	C	4500
e4	D	7000
e5	E	6700

Insert into Employee
Value < e5, E, 6700 >

SerializabilityRecoverabilityDependency

1.	T_1	T_2	2.	T_1	T_2	3.	T_1	T_2	4.	T_1	T_2
	$W(A)$			$W(A)$			$W(A)$			$W(A)$	
	$\vdots$			Commit			rollback				
	Commit	$R(A)$			$R(A)$		undo all modifications	$R(A)$			
					$\vdots$						No dependency
				No dependency			No dependency				

Yes - dependency.
 T_2 depends on T_1 .
Uncommitted/Dirty Read.

5.	T_1	T_2	6.	T_1	T_2
	$W(A)$			$W(A)$	
		$W(A)$			$W(B)$
		$R(A)$			$R(A)$
				$R(B)$	

Yes - dependency.
 T_2 - depend on T_1 .
 T_1 - depend on T_2 .

No dependency.
No uncommitted read.

T_1	T_2
$R(A)$	
$\vdots$	
$W(A)$	
	$R(A)$
	$\vdots$
	Commit

{ Irrecoverable }

↑ failure

Recoverable Schedule: A recoverable schedule is one, for each pair of transactions T_i and T_j such that, T_j read a data item that was previously written T_i then Commit of T_i appear before commit of T_j .

T_i	T_j
$W(A)$	
	$R(A)$
C/R	<u>Commit</u>

If T_2 depends on T_1 then commit of T_2 must be delay until commit/rollback of T_1 .

Need to address the effect of transaction failure on concurrently running transactions.

* Recoverable Schedule: Transaction T_j reads a data item previously written by transaction T_i , then the commit operation of T_i appears before commit operation of T_j .

* The following schedule is not recoverable:

T_8	T_9
read(A)	
write(A)	Read(A)
	<u>Commit</u>
read(B)	

If T_8 should abort, T_9 would have read (and possibly, shown to a user) an inconsistent database state. Hence database must ensure that Schedules are recoverable.

Example.

T_1	T_2
$W(A)$	
	$R(A)$
	$C_2(\text{commit})$
Rollback	

Irrecoverable

T_1	T_2
$W(A)$	
C/R	$R(A)$
	Rollback

Recoverable

T_1	T_2
$W(A)$	
	$R(A)$
	C_2
C_1	

Irrecoverable

T_1	T_2
$W(A)$	$W(A)$
	$R(A)$
	<u>Commit</u>
C/R	

Recoverable

T_1	T_2
$W(A)$	
	$R(A)$
C/R	C/R

Recoverable

Note: Recoverable Schedule may or may not be free from WR problem, RW problem, WW problem.

T ₁	T ₂	T ₁	T ₂	T ₁	T ₂
R(A)	W(A)	W(A)	W(A)	R(A)	
	Commit		Commit	W(B)	R(B)
Commit		Commit		Commit	R(B)
Recoverable but RW problem.		Recoverable but WW problem.		Recoverable But WR problem.	
					Commit

Cascading Rollbacks: a single transaction failure leads to a series of transaction rollbacks. Consider the following schedule where none of the transactions has yet committed (so the schedule is recoverable).

T ₁₀	T ₁₁	T ₁₂
read(A)		
read(B)		
W(A)	read(A)	
	write(A)	read(A)
abort		

* If T₁₀ fails, T₁₁ and T₁₂ must also be rolled back.

* Can lead to the undoing of a significant amount of work.

Cascades Schedule: Cascading rollback cannot occur.

- * For each pair of transactions T_i and T_j such that T_j reads data item previously written by T_i and the commit operation of T_i appears before the read operation of T_j.
- * Every Cascades Schedule is also recoverable.

T ₁	T ₂
W(A)	
C/R	R(A)
Cascades Schedule	

* No WR Problem

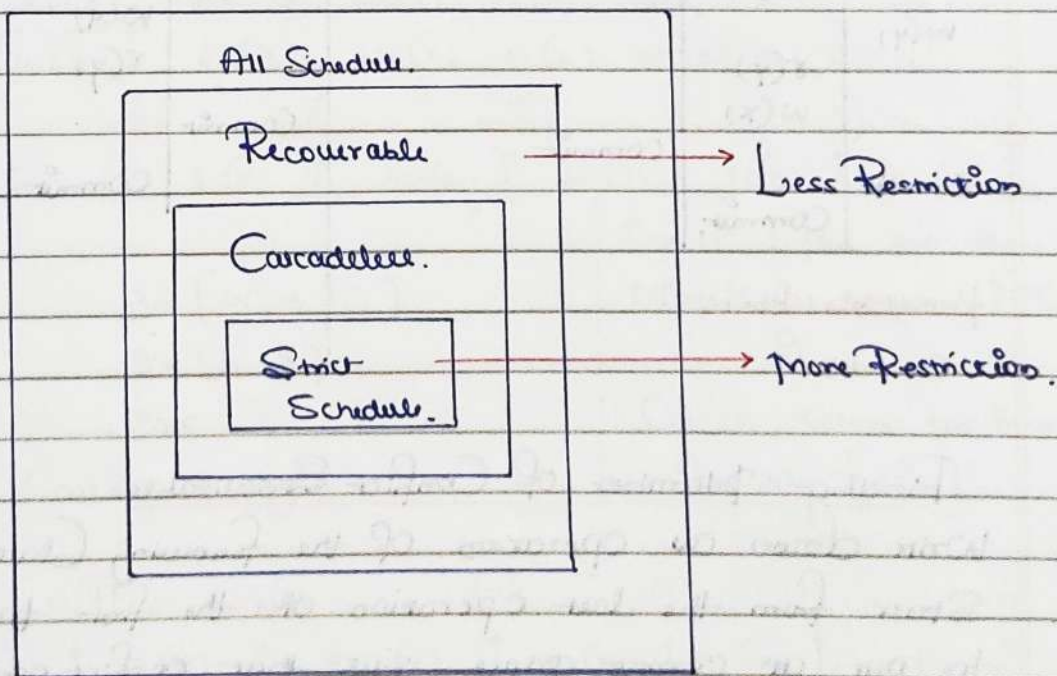
* No uncommitted (dirty) read

* No cascading rollback

Note: Cascadable schedule may or may not be free from RW problem, HW problem.

<u>T₁</u>	<u>T₂</u>		<u>T₁</u>	<u>T₂</u>	
R(A)	W(A)	Cascades,1	W(A)		Cascades,2
	Commit	but Rno		W(A),	
		problem.		Commit	but two problems.
Commit			Commit		

1. T_1	T_2	2. T_1	T_2	3. T_1	T_2
$w(A)$		$w(A)$		$w(A)$	
	$R(A)$	c/r		c/r	
c/r			$R(A)$		$R(A)/w(A)$
	Commit.				
Recoverable Schedule.		Cascadable Schedule.		Strict Recoverable	
		- WW problem			
		- RW problem			



Q1. $r_1(x), r_2(z), r_1(z), r_3(x), r_3(y), w_1(x), w_3(y), r_2(y), w_2(z), w_2(y), C_1, C_2, C_3$.

T_1	T_2	T_3
$r(x)$	$r(z)$	
$r(z)$		$r(x)$
		$r(y)$
$w(x)$		$w(y)$
	$r(y)$ $w(z)$ $w(y)$	
Commit	Commit	Commit

∴ Not
Recoverable.

Q2. $r_3(x) r_1(x) w_3(x) r_2(x) w_1(y) r_2(y)$ Q3. $r_1(x) r_2(x) w_1(y) w_2(y) r_2(y) C_1$
 $w_2(x) C_3, C_2$

T_1	T_2	T_3
		$r(x)$
$r(x)$		$w(x)$
	$r(x)$	
$w(y)$	$r(y)$ $w(x)$	
Commit	Commit	Commit

Recoverable but not
Cascadable.

T_1	T_2
$r(x)$	$r(x)$
$w(y)$	$w(y)$
$r(y)$	$r(y)$
Commit	Commit

Recoverable ✓
Cascadable ✓
Strict Recoverable x
- No Cascading rollback

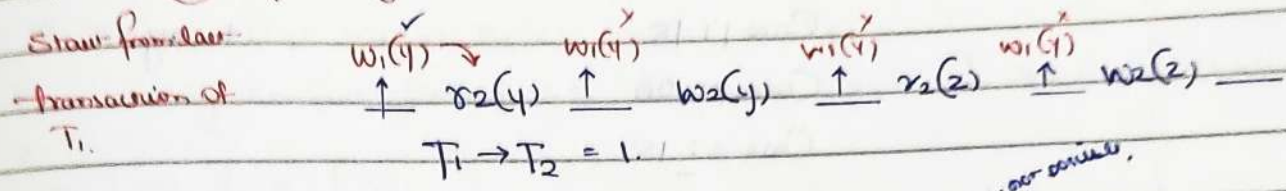
Finding Number of Conflict Serializable

- Write down all operations of the following (later) transactions.
- Start from the last operation of the first transaction and try to put at correct place such that conflict operation order must be maintained same as transaction order.

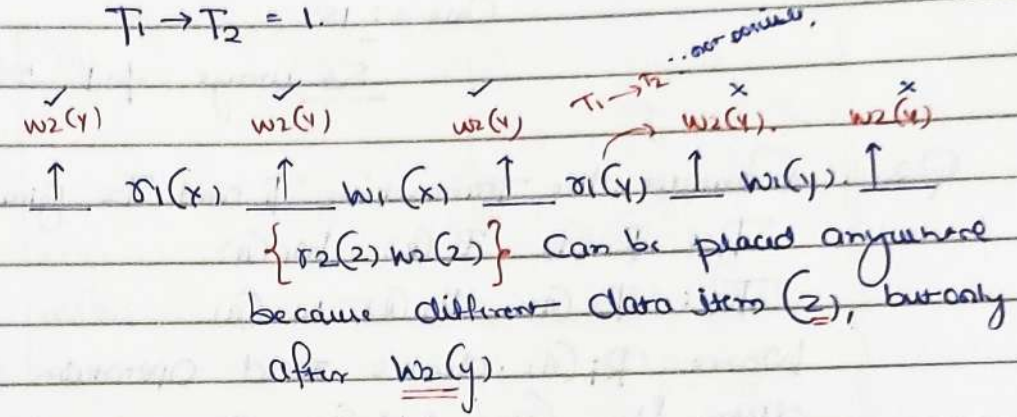
Q1. Two transactions are given: $T_1: r_1(x) w_1(x) r_1(y) w_1(y)$
 $T_2: r_2(y) w_2(y) r_2(z) w_2(z)$

Where $r_i(v)$ denote a read operation by transaction T_i on a variable v and $w_i(v)$ denote a write operation by transaction T_i on a variable v . The total no of conflict serializable schedules that can be formed by T_1 and T_2 is _____

Ans. $T_1 \rightarrow T_2$ following



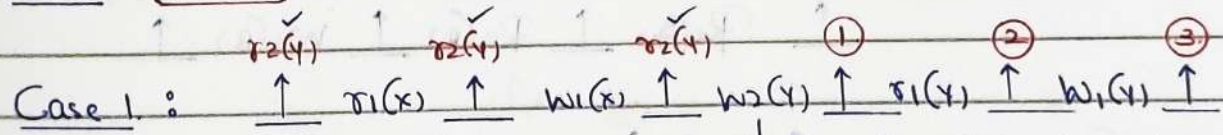
$T_2 \rightarrow T_1$
Start from last transaction of T_2



Case 1: $r_1(x) \quad w_1(x) \quad w_2(y) \quad r_1(y) \quad w_1(y)$

Case 2: $r_1(x) \quad w_2(y) \quad w_1(x) \quad r_1(y) \quad w_1(y)$

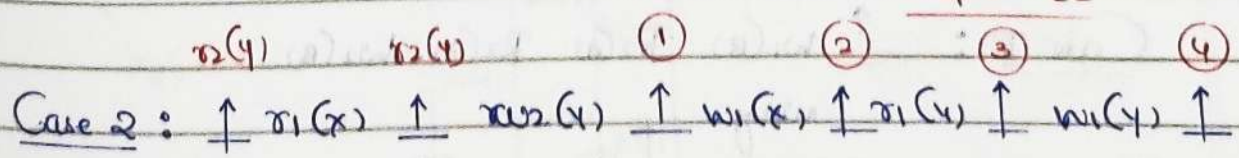
Case 3: $w_2(y) \quad r_1(x) \quad w_1(x) \quad r_1(y) \quad w_1(y)$



$3 \times [3C_1 + 3C_2]$
 $3 \times [3 + 3]$
 3×6

Case 1 = 18 ways

Out of 3 place put them $r_2(z) w_2(z)$ together $[3C_1]$
or
Out of 3 place put them Separately $[3C_2]$
 $3C_1 + 3C_2$



2 ways $\Rightarrow 2 \times [4C_1 + 4C_2]$
 $2 \times [4 + 6]$
 $= 20 \text{ ways}$

Case 3: $\uparrow^{(1)} w_2(y) \uparrow^{(1)} r_1(x) \uparrow^{(2)} w_1(x) \uparrow^{(3)} r_1(y) \uparrow^{(4)} w_1(y) \uparrow^{(5)}$

$$1 \times [5C_1 + 5C_2]$$

$$5 + 10 = 15 \text{ ways}$$

$T_2 \rightarrow T_1$

Case 1: 18

Case 2: 20

Case 3: 15

$$\underline{53 \text{ ways}} + 1 \Rightarrow \underline{54 \text{ ways}}$$

$T_1 \rightarrow T_2$

1 way

Q2. Consider the transaction T_1 and T_2 given below:

$T_1: R_1(A) \quad R_1(B) \quad W_1(B)$

$T_2: R_2(A) \quad R_2(B) \quad W_2(B)$

Where $R_i(A)$ denote read operation by transaction T_i on a data item (A) $W_i(B)$ denote a write operation on transaction T_i on data item (B).

The total number of Conflict Serializable Schedule is _____.

Ans.

$T_1 \rightarrow T_2$ $\uparrow^{(1)} w_1(B) \uparrow^{(2)} R_2(A) \uparrow^{(3)} R_2(B) \uparrow^{(4)} w_2(B) \uparrow^{(5)} w_1(B)$

Case I: $\uparrow^{(1)} R_2(A) \uparrow^{(2)} w_1(B) \quad R_2(B) \quad W_2(B)$

$$2C_1 + 2C_2$$

$$\Rightarrow 2 + 1 = 3 \text{ ways}$$

Out of 2 places, place them together

$2C_1$ or

Out of 2 spot, place them Separately $2C_2$

Case II: $\uparrow w_1(B) R_2(A) R_2(B) W_2(B)$

1 way

$T_1 \rightarrow T_2$

Case I: 3 ways

Case II: 1 way
4 ways

Because T_1 and T_2 are exactly same

$T_2 \rightarrow T_1$: 4 ways

$$\therefore 4 + 4 \Rightarrow \underline{8 \text{ ways}}$$

Total Conflict Serializable : 8

Non Serial Conflict-Serializable : 8 - 2

= 6

Serial Schedule

Q3 Consider the given Schedule:

S: $r_1(x), r_2(y), w_3(y), r_4(x), w_4(z), w_3(y)$.

How many conflict serializable schedules exist for the above schedule S?

Ans.

T_1	T_2	T_3	T_4
$r(x)$	$r(y)$	$w(y)$	$r(x)$
			$w(z)$
		$w(y)$	

T_1

T_2

T_4

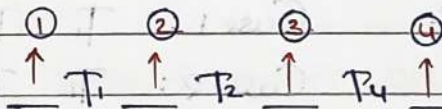
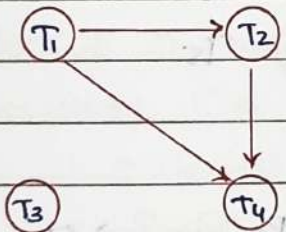
T_3

T_1 and T_4 can be placed anywhere.

$$= T_2 _ T_3 = 3! \times 2! = 12 \text{ ways}$$

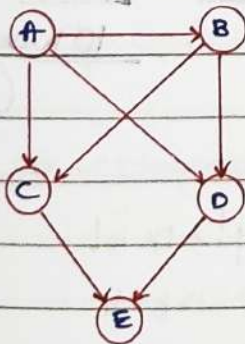
Topological Sorting Questions

1.



Ans = 4

2.

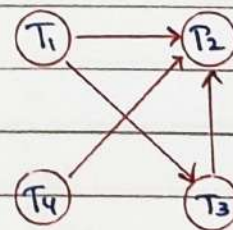


ABCDE } 2 ways
ABDCE }
Ans = 2

3.

$R_4(x), R_2(x), R_3(x), w_1(y), w_2(x), R_3(y), w_2(y)$

T_1	T_2	T_3	T_4
	$R(x)$	$R(x)$	$R(x)$
$w(y)$	$w(x)$	$R(y)$	
	$w(y)$		



$\langle T_1, T_4, T_3, T_2 \rangle$
 $\langle T_4, T_1, T_3, T_2 \rangle$
 $\langle T_1, T_3, T_4, T_2 \rangle$

Ans

Q4. Consider the following Schedule

$S = r_1(P), r_2(S), w_1(Q), r_2(Q), r_4(Q), w_2(R), r_5(R), w_4(T), r_5(T), w_5(Q)$.

How many Serial Schedules are possible which will be view equivalent?

Ans

T_1	T_2	T_3	T_4	T_5
$r(P)$		$r(S)$		
$w(Q)$	$r(Q)$		$r(Q)$	
	$w(R)$			$r(R)$
			$w(T)$	$r(T)$
				$w(Q)$

① Initial Read : $P : T_1$ $S : T_3$

② Final Write : $Q : T_5 \rightarrow T_1 \rightarrow T_5$

③ Updated Read (Write-Read Sequence)

$w_1(Q) \ r_2(Q) : T_1 \rightarrow T_2$

$w_1(Q) \ r_4(Q) : T_1 \rightarrow T_4$

$w_2(R) \ r_5(R) : T_2 \rightarrow T_5$

$w_4(T) \ r_5(T) : T_4 \rightarrow T_5$

$T_1 \rightarrow T_5$

$T_1 \rightarrow T_2$

$T_1 \rightarrow T_4$

$T_2 \rightarrow T_5$

$T_4 \rightarrow T_5$

$T_1 \rightarrow T_2 \rightarrow T_5$

T_4 comes after T_1 and before T_5 .

Case 1 : $T_1 \ T_4 \ T_2 \ T_5$

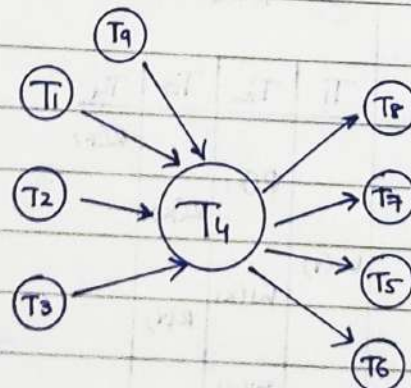
Case 2 : $T_1 \ T_2 \ T_4 \ T_5$

T_3 Can be placed anywhere.

Case I : ① T_1 ② T_4 ③ T_2 ④ T_5 ⑤ $T_3 \rightarrow S$

Case II : ① T_1 ② T_2 ③ T_4 ④ T_5 ⑤ $T_3 \rightarrow S$

10 Ways (Ans)



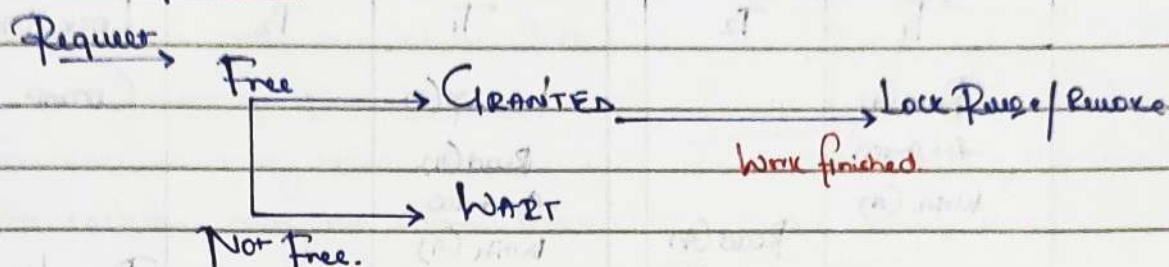
$4! \times 1 \times 4!$

$\Rightarrow 24 \times 24$

$\Rightarrow \underline{\underline{576}}$

Implementation of Concurrency Control.

Lock based Protocol



Procedure:

Before using any data item, transactions should request for a lock, if lock is free (lock not taken by any data item) then it will be granted, otherwise transactions has to wait (if busy).

Types of lock:

		Same data item	Tj	
			S	X
1. Shared lock (S) → Only read	Ti	S	Yes	No
2. Exclusive lock (X) → write(A) / read(A) / write(A)		X	No	No

* A lock is a mechanism to control concurrent access to a data item.

* Data items can be locked in two modes:

1. Exclusive (X) mode

2. Shared (S) mode

* Lock requests are made to Concurrency-Control manager. Transactions can proceed only after request is granted.

Lock-compatibility matrix:

data item (A)	S	X
S	True	False
X	False	False

* A transaction may be generated a lock on an item if the requested lock is compatible with lock already held on the item by other transactions.

* Any number of transactions can hold shared locks on an item.

- But if any transaction holds an exclusive on the item, no other transaction may hold any lock on that item.

T ₁	T ₂	T ₁	T ₂	Lock Manager
Read(A) A = A - 100 Write(A)		<u>Lock-x(A)</u> Read(A) A = A - 100 Write(A) <u>Unlock-x(A)</u>		Grant-x(A, T ₁)
	Read(A) Read(C)			Reuse/Remove-x(A, T ₁)
Read(B) B = B + 100 Write(B)			<u>Lock-S(A)</u> Read(A)	Grant-S(A, T ₂)
			<u>Unlock-S(A)</u>	Remove-S(A, T ₂)
			<u>Lock-S(C)</u> Read(C)	Grant-S(C, T ₂)
			<u>Unlock-S(C)</u>	Remove-S(C, T ₂)
		<u>Lock-x(B)</u> Read(B) B = B + 100 Write(B) <u>Unlock-x(B)</u>		Grant-x(B, T ₁)
				Remove-x(B, T ₁)

- A locking protocol is a set of rules followed by all transactions while requesting and releasing locks.
- Locking protocols enforce serializability by restricting the set of possible schedules.

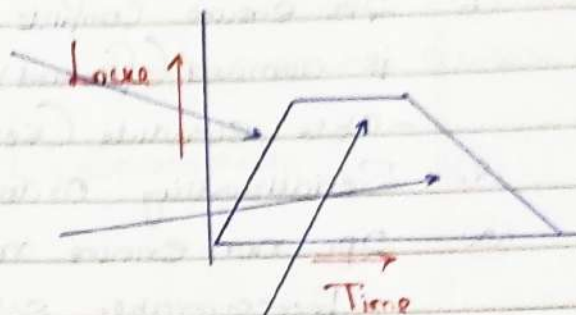
Two Phase Locking Protocol (2PL)

Lock and unlock request done in two phase

1. Growing phase (Acquire locks)
2. Shrinking phase (Release locks)

Each transaction first finish its growing phase then start shrinking phase.

- * A Protocol which ensures Conflict Serializable Schedule.
- * Phase 1: Growing Phase
 - * Transactions may obtain lock.
 - * Transactions may not release lock.
- * Phase 2: Shrinking Phase
 - * Transaction may release locks
 - * Transaction may not obtain lock.
- * The protocol assures Serializability. It can be proved that the transactions can be serialized in the order of their lock points (i.e. the point where a transaction acquired its final lock).



T ₁	T ₂	T ₁	T ₂	Lock Manager
Read(A) A = A - 100 Write(A)		Lock-X(A) Read(A) A = A - 100 Write(A)		✓ Grant
	Read(A) Read(C)		Lock-S(A)	✗ No
Read(B) B = B + 100 Write(B)		Lock-S(B) Unlock-X(A)		✓ Release-X(A, T ₁)
			Lock-S(A) Read(A)	✓ Yes Grant
			Lock-S(C)	✓ Yes Grant
			Unlock-S(A)	✗ Release.
		Read(B) B = B + 100 Write(B) Unlock-S(B)		✓

Lock point: Position of last lock operation or first-unlock operation
Or

Position from where shrinking phase of the transaction start.

Important Points about 2PL:

- ① 2PL ensure Conflict Serializability (Serializability). If a schedule is allowed (followed) by 2PL then it ensure Conflict Serializable Schedule (Serializability).
- ② Serializability Order is determined by Lock point.
- ③ 2PL not ensure recoverability.

Irrecoverable Schedule followed by 2PL

T ₁	T ₂
RG(A)	
W(A)	
	RG(A)
	Commit
Commit	

Irrecoverable Schedule

T ₁	T ₂
X(A)	
RG(A)	
W(A)	
Unlock(A)	
	SG(A)
	RG(A)
	Unlock S(A)
	Commit
Commit	

Irrecoverable Schedule
But allowed (followed)
by 2PL

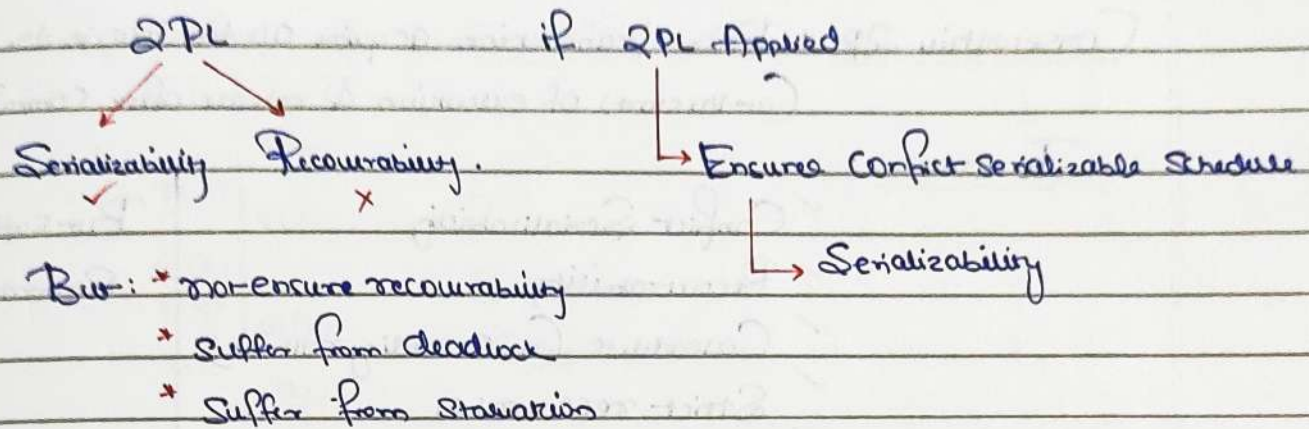
①	T ₁	T ₂	T ₁	T ₂	②	T ₁	T ₂	T ₁	T ₂
	W(A)		X(A)			RG(A)		S(A)	
		R(B)	W(A)				W(B)		RG(A)
	W(B)		denied by T ₂ → X(B)	S(B)		R(B)		denied by T ₂ → S(B)	X(B)
		R(A)	R(B)	R(B)		W(A)			W(B)
			SG(A) ← denied by T ₁						X(A) ← denied by T ₁

∴ Deadlock

∴ Deadlock

- ④ 2PL suffers from (may not be free from) deadlock.
- ⑤ 2PL suffers from Starvation.

	T ₁	T ₂	T ₃	T ₄
denied by T ₂ →	X(A)	S(A)		
denied by T ₃ →	X(A)	U(A)		
denied by T ₄ →	X(A)		U(A)	S(A)
✓ Granted →	X(A)			U(A)



Strict 2PL : 2PL + All exclusive lock (X lock) taken by the transaction must be held until commit/rollback.

- X lock Release after Commit/rollback
- It ensures :
 - * Conflict-Serializable
 - * recoverable Schedule
 - * Cascades (no cascading rollback)
 - * Strict recoverable
- Suffers from: deadlock and starvation.

Rigorous 2PL : 2PL + All locks (Shared[S] and Exclusive[X]) must be held by the transaction until commit/rollback.

→ Suffers from: deadlock and starvation.

Two Phase Locking Protocol (Continued)

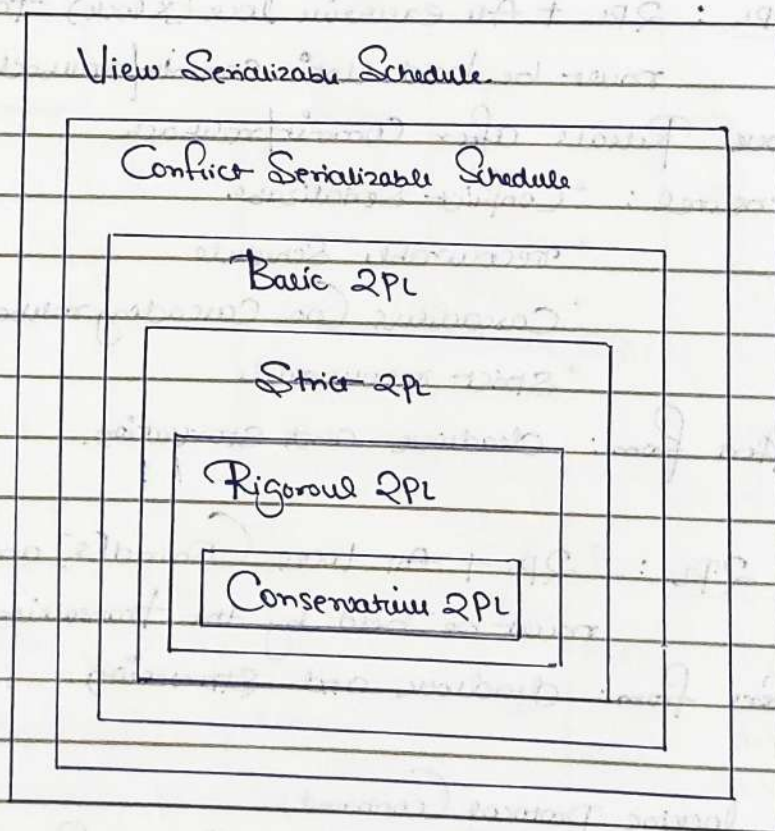
- * Two phase locking does not ensure freedom from deadlocks.
- * Extensions to basic two-phase locking needed to ensure recoverability of freedom from cascading roll back
- ① Strict 2phase locking - a transaction must hold all its exclusive locks until commit/rollback.
 - * Ensures recoverability and avoids cascading roll back.
- ② Rigorous two phase locking: a transaction must hold all locks until commit/abort.
 - * Transactions can be serialized in the order in which they commit.
- * Most database implement rigorous 2-phase, but refer to it as simply 2-phase.

Conservative 2PL: Each transaction acquire all the lock in the beginning (at the start) of execution & release after commit.

It ensures:

- ✓ Conflict Serializability
- ✓ Recoverability
- ✓ Cascadeless (no cascading rollback)
- ✓ Strict recoverable
- ✓ No deadlock

But suffers from Starvation.



- Q1. Consider the following database schedule with two transactions T_1 and T_2 . $S = r_2(x), w_1(x), r_2(x), w_1(x), w_2(x), a_1, a_2$.
 where $r_i(z)$ denotes a read operation by transaction T_i on a variable z , $w_i(z)$ denotes write operation of variable z and a_i denotes an abort by transaction T_i .
 Which of the following statements about schedule is true?
- Ans. S does not have a cascading abort.

$r_2(x), r_1(x), r_2(y), w_1(x), r_1(y), w_2(x), a_1, a_2$

T_1 | T_2

$r(x)$ | $r(x)$

$r(x)$ | $r(y)$

$w(x)$ | $r(y)$

$r(y)$ | $w(x)$

a_1 | a_2

✓ Recoverable

✓ Cascadeless

✗ Strict Recoverable

Q2. Let S be the following schedule of operations of three transactions T_1, T_2, T_3 in relational database system.

$R_2(y), R_1(x), R_3(z), R_1(y), w_1(x), R_2(z), w_2(y), R_3(x), w_3(x)$

Consider the statements P and Q below.

$P: S$ is conflict serializable.

$Q: \text{If } T_3 \text{ commits before } T_1 \text{ finishes, then } S \text{ is recoverable}$

Which of the following choice is correct?

Ans

T_1 | T_2 | T_3

$R(x)$ | $R(y)$ |

$R(y)$ | $R(z)$ | $R(z)$

$w(x)$ | $R(z)$ | $R(x)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

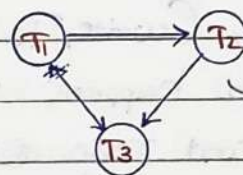
$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$

$w(x)$ | $w(y)$ | $w(z)$



Conflict Serializable

Not

Recoverable

$\Rightarrow P$ is true and Q is false.

Undo and Redo

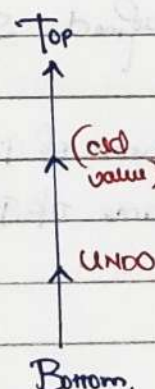
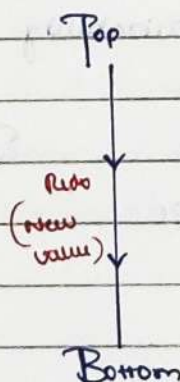
Transaction Number (Operation, data item, Old value, New value).

(OV) (NV)
(X, 5, 7)

(OV) (NV)
(X, 7, 11)

Redo: X: 5 $\neq$ 11

$\rightarrow$ X = 11



Undo:

X: 11 $\neq$ 5

X = 5

- * Those transactions commit before Check Point not required any Redo operation.
- * Those transactions commit after Check point required redo operation.
- * Those transactions not commit require undo operation.
- * If T_1 commit then Redo
- * If Any transaction that not commit require Undo operation.
- * Log based recovery.

Q3. Consider a Simple Checkpointing Protocol and the following set of operations in the log.

(Start, T_4); (write, T_4 , y, 2, 3); (Start, T_1);

(Commit, T_4); (write, T_1 , z, 5, 7);

{Checkpoint}

(Start, T_2), (write, T_2 , x, 1, 9); (Commit, T_2)

(Start, T_3), (write, T_3 , z, 7, 2);

If a crash happens now and the system tries to recover using both undo and redo operations, what are the contents of the undo and redo list?

Anc Undo: T_3, T_1 Redo: T_2

Time Stamp Protocol

- * A unique time stamp value assigned to each transaction when they arrive in the system.
- * Based on this time stamp determines the serializability order. (TSP predefined serializability order based on timestamp).

eg:

Time Stamp of T_1 : 10

Time Stamp of T_2 : 20

Serializability: $T_1 \rightarrow T_2$

Order

Older

Transaction

Younger Transaction

Transaction : T_1 T_2 T_3 T_4 T_5 T_6
 if TimeStamp : 10 30 20 40 60 50
 of Transaction

Serializability Order: $(T_1) \rightarrow (T_3) \rightarrow (T_2) \rightarrow (T_4) \rightarrow (T_6) \rightarrow (T_5)$
 (Time Stamp) (Older transaction) (Younger transaction)

eg. $Ts(T_1) > Ts(T_2)$ Serializability Order: $T_2 \rightarrow (T_1)$
 $Ts(T_1) < Ts(T_2)$ Serializability Order: $T_1 \rightarrow (T_2)$

- * Each transaction T_i is issued a timestamp $Ts(T_i)$ when it enters the system.
- * Each transaction has a unique timestamp.
- * Newer transactions have transaction timestamp strictly greater than earlier ones.
- * Timestamp could be based on a logical counter.
 - Realtime may not be unique.
 - Can use (even clock time, logical counter) to ensure.
- * Time Stamp based protocols manage current execution such that time-stamp order = Serializability Order.

The timestamp Ordering (TSO) Protocol

- * Maintains for each data Q two timestamp values:
 1. W-timestamp(Q) is the largest time-stamp of any transaction that executed write(Q) successfully.
 2. R-timestamp(Q) is the largest time-stamp of any transaction that executed read(Q) successfully.
- * Imposes rule on read and write operations to ensure that:
 - * Any conflicting operations are executed in timestamp order.
 - * Out of order transactions operations cause transaction rollback.

Two types of Time Stamp:

(1) Transactions Time Stamp

(2) Data item - time Stamp

(i) Read - Time Stamp (Q) $R_{TS}(Q)$ (ii) Write - Time Stamp (Q) $W_{TS}(Q)$ Read - Time Stamp (Q) : denotes the higher transaction time Stamp that perform Read (Q) operation Successfully.

(10) T_1	(20) T_2	(30) T_3
R(A)		
	R(A)	
		R(A)

Initially $R_{TS} = 0$ $R_{TS} = 10, \max(0, 10)$ $R_{TS} = 20, \max(10, 20)$ $R_{TS} = 30, \max(20, 30)$ $R_{TS}(A) = 30$ Write - Time Stamp (Q) : denotes the higher transaction time Stamp that perform write (Q) operation Successfully.

(10) T_1	(20) T_2	(30) T_3
W(A)		
	W(A)	
		W(A)

 $W_{TS} = 0$ initially $W_{TS} = 10, \max(0, 10)$ $W_{TS} = 20, \max(10, 20)$ $W_{TS} = 30, \max(20, 30)$ $W_{TS}(A) = 30$ Conflict Operation

Same data item

 $R(A) \rightarrow W(A)$ $W(A) \rightarrow R(A)$ $W(A) \rightarrow W(A)$ Non Conflict Operation $R(A) \rightarrow R(A)$ (different data item) $R(A) \rightarrow W(B)$ $W(B) \rightarrow R(A)$ $W(B) \rightarrow W(A)$ Read (Q) : T_i Transaction T_i wants to perform read (Q) operation $TS(T_i) < W_{TS}(Q)$: Read operations and T_i rollback and restart with new Stamp.

T_i : Write(Q) : Transaction T_i wants to perform write(Q) Operation.

$TS(T_i) < RTS(Q)$ } Write Operation & Transaction Rollback
 $TS(T_i) < WTS(Q)$ } Reject and restart with new timer.

(10) T_1	(20) T_2	(30) T_3
W(A)		W(A)
	W(A)	

NOT TSP.

$$TS(T_2) < WTS(A)$$

$$20 < 30$$

Not allowed

I T_i - Read(Q) (Transaction T_i issue R(Q) Operation)

(i) If $TS(T_i) < WTS(Q)$: Read Operation and T_i rollback/abort and restart with new transaction.

(ii) If $TS(T_i) \geq WTS(Q)$: Read Operation is allowed,
 And Set Read- $TS(Q) = \max[RTS(Q), TS(T_i)]$

II. T_i - Write(Q) (Transaction T_i issue write(Q) Operation)

(i) If $TS(T_i) < RTS(Q)$: Write Operation reject and T_i rollback

(ii) If $TS(T_i) < WTS(Q)$: Write Operation reject and T_i rollback.

(iii) Otherwise execute write(Q) operation.

Set Read- $WTS(Q) = TS(T_i)$.

→ Suppose a transaction T_i issue a read(Q)

① If $TS(T_i) \leq W\text{-timestamp}(Q)$, then T_i needs to read a value of Q that was already overwritten.

Hence the read Operation is rejected and T_i is rolled back and restart with new timestamp.

② If $TS(T_i) \geq W\text{-timestamp}(Q)$, then read Operation is executed, and R-timestamp(Q) is set to $\max(R\text{-timestamp}(Q), TS(T_i))$.

→ Suppose a transaction T_i issues write(Q)

① If $Ts(T_i) < R\text{-timestamp}(Q)$, then the value of Q that T_i is producing was needed previously, and the system assumed that the value would never be produced. Hence the write operation is rejected and T_i is rolled back.

② If $Ts(T_i) < W\text{-timestamp}(Q)$ then T_i is attempting to write an obsolete value of Q .

Hence the write operation is rejected, and T_i is rolled back.

③ Otherwise the write operation is executed and $W\text{-timestamp}(Q)$ is set to $Ts(T_i)$.

TSP: $Ts(T_1) < Ts(T_2)$

If $Ts(T_1) : 10$

Order: $T_1 \rightarrow T_2$

If $Ts(T_2) : 20$

T_1 followed by T_2

Note:

Then all Conflicting Operations must be executed in the order T_1 followed by T_2 (same as Serializability order)

— if yes then allowed under TSP

— if no then not allowed under TSP

(10)	(20)	(30)	(10)	(20)	(30)	(10)	(20)	(30)	(10)	(20)	(30)
T_1	T_2	T_3	T_1	T_2	T_3	T_1	T_2	T_3	T_1	T_2	T_3
R(A)			R(A)			R(A)			W(A)		W(A)
	W(A)				W(A)			R(A)		W(B)	
		R(A)		W(B)			R(A)			R(B)	

$T_1 \rightarrow T_2 \rightarrow T_3$

"Yes TSP"

$T_1 \rightarrow T_2 \rightarrow T_3$

"Yes"

$T_1 \rightarrow T_2 \rightarrow T_3$

"Yes"

$T_1 \rightarrow T_2 \rightarrow T_3$

"Yes"

(10)	(20)	(30)	(10)	(20)	(30)
T_1	T_2	T_3	T_1	T_2	T_3
W(A)				W(A)	
	R(A)				
		W(A)	W(A)		W(A)
	W(A)				

$T_1 \rightarrow T_2 \rightarrow T_3$
Not Allowed
 $Ts(T_2) < WTs(A)$ not allowed
 T_2 rollback & restart

Why Restart with higher value?

(10)	(20)
T_1	T_2
	$R(A)$
$W(A)$	

If again restart with
Same time Stamp.

(10)	(20)
T_1	T_2
	$R(A)$
$W(A)$	

again not
allowed under TSP
again rollback.

if higher timestamp?

(20)	(30)
T_2	T_1
$R(A)$	
	$W(A)$

yes allowed
under TSP.

$T_2 \rightarrow T_1$
& Conflict operation
 $T_2 \rightarrow T_1$.

Important Point about TSP:

1. If Schedule followed by TSP then ensure Conflict Serializable
2. TSP not ensure recoverability

(10)	(20)
T_1	T_2
$W(A)$	
$T_1 \rightarrow T_2$	$R(A)$
Commit	Commit

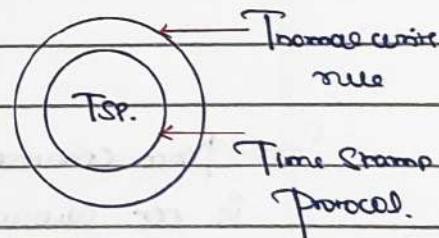
- allowed under TSP

but irreplaceable schedule

3. TSP free from deadlock.
4. Starvation may or may not occur

Thomas Write Rule (View Serializability)

- * If S allowed by TSP then already it is allowed by Thomas write rule
- * If some schedule not allowed by TSP then it may be allowed by Thomas write rule.



→ Some little modifications in TSP

Allowed Obsolete write. But obsolete write not allowed under TSP.

$T_1: Read(Q) \rightarrow$ Same as TSP.

$T_2(T_1) < hrs(Q):$ Read operation reject and rollback.

$T_i: \text{Write}(Q)$

$Ts(T_i) < WTS(Q)$: write operation and no rollback (allowed case, ignored).

$Ts(T_i) < RTS(Q)$: Reject & T_i rollback.

Thomas' Write Rule (Formal Definition)

Modified version of the time-stamping-ordering protocol in which obsolete write operations may be ignored under certain circumstances.

When T_i attempts to write data item Q , if $Ts(T_i) < W\text{-timestamp}(Q)$, then T_i is attempting to write an obsolete value of Q .

— Rather than rolling back T_i as the time-stamp ordering protocol would have done, this {write} operation can be ignored.

Otherwise this protocol is same as the time-stamp ordering protocol.

Thomas' Write Rule allows greater potential concurrency.

— Allows some view-serializable schedules that are not conflict-serializable.

(10)	(20)		T_1	T_2
$R(A)$			$R(A)$	
	$W(A)$			
Obsolete write $\rightarrow W(A)$		But allowed under Thomas write rule.	$R(A)$	
		$T_i \Rightarrow W(A)$: ignored	$W(A)$	
		rollback.		$W(A)$
		allowed under TWR.		

$Ts(T_1) < WTS(A)$
 $10 < 20$; not allowed under TSP

→ More concurrency means this schedule is not conflict serializable, this is not allowed under TSP but allowed by Thomas write rule.

eg.

T_1	T_2	T_3
$R(A)$		
	$N(A)$	
$W(A)$		
		$W(A)$

Observe read.

This is allowed under Thomas write rule.

(10)	(20)
T_1	T_2
R(B)	W(B)
	W(A)
W(A)	
R(A)	

Clock Rule:

$T_1: W(A) \quad TS(T_1) < WTS(A) \rightarrow$ yes allowed in Two.

$T_1: R(A) \rightarrow TS(T_1) < WTS(A) \rightarrow$ not in Two.

$T_1 \rightarrow T_2$

Not TSP, Not Two

Time Stamp protocol: ensure Serializability, deadlock free, but Starvation Possible.

Deadlock Prevention Algorithm:

- (i) Wait-Die (ii) Wound-Wait
Older Younger.

$T_1(10)$	$T_2(20)$
R(A)	W(A) <u>Not in TSP</u>
W(A)	<u>But in Two</u>

$TS(T_1) < TS(T_2)$
 $T_1 \rightarrow T_2$

Strict Time Stamp Ordering Protocol = TSP + Strict Schedule.

It Ensures: Serializability
Recoverability
Cascading (no cascading rollback)
Strict Recoverability

Q1. In which of the following lock scheme deadlock cannot occur?
Ans Conservative 2PL

Q2. Consider the following schedule: $r_1(x), r_2(y), r_2(x), w_1(z), r_1(y), w_3(y)$
 $r_2(z), w_2(y), w_3(x)$.

Which of the time stamp ordering not allowed to execute schedule using Thomas Write Rule time stamping ordering protocol?

Ans $(T_1, T_2, T_3) = (10, 20, 30)$.

Q3. Consider the two statements about Database Transaction Schedules:

I. Strict two phase locking protocol generated Conflict Serializable Schedules that are also recoverable.

II. Timestamp Ordering Concurrency Control protocol with Thomas write rule can generate view Serializable Schedules that are not conflict serializable.

Which of above statements is/are true?

Ans Both I and II.

Q4. Which of the following Concurrency Control Protocols ensure both Conflict Serializability and freedom from deadlock?

I. 2-phase locking

II. Time Stamp ordering.

Ans II Only.